

GEODOMISI Ltd. - Dr. Costas Sachpazis
 Civil & Geotechnical Engineering Consulting Company for
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Project: Steel Member Design in Biaxial Bending And Axial
 Compression Example, in accordance with EN1993-1-
 1:2005 incorporating Corrigenda February 2006 and April
 2009 and the recommended values

Job Ref.

Section

Civil & Geotechnical Engineering

Sheet no./rev. 1

Calc. by

Dr. C. Sachpazis

Date

09/02/2014

Chk'd by

Date

App'd by

Date

STEEL MEMBER DESIGN (EN1993-1-1:2005)

**In accordance with EN1993-1-1:2005 incorporating Corrigenda February 2006
 and April 2009 and the recommended values**

Section details

Section type;

UKC 356x406x287 (Corus Advance)

Steel grade;

S275

**From table 3.1: Nominal values of yield strength f_y and ultimate tensile strength f_u for hot rolled
 structural steel**

Nominal thickness of element;

$t = \max(t_f, t_w) = 36.5$ mm

Nominal yield strength;

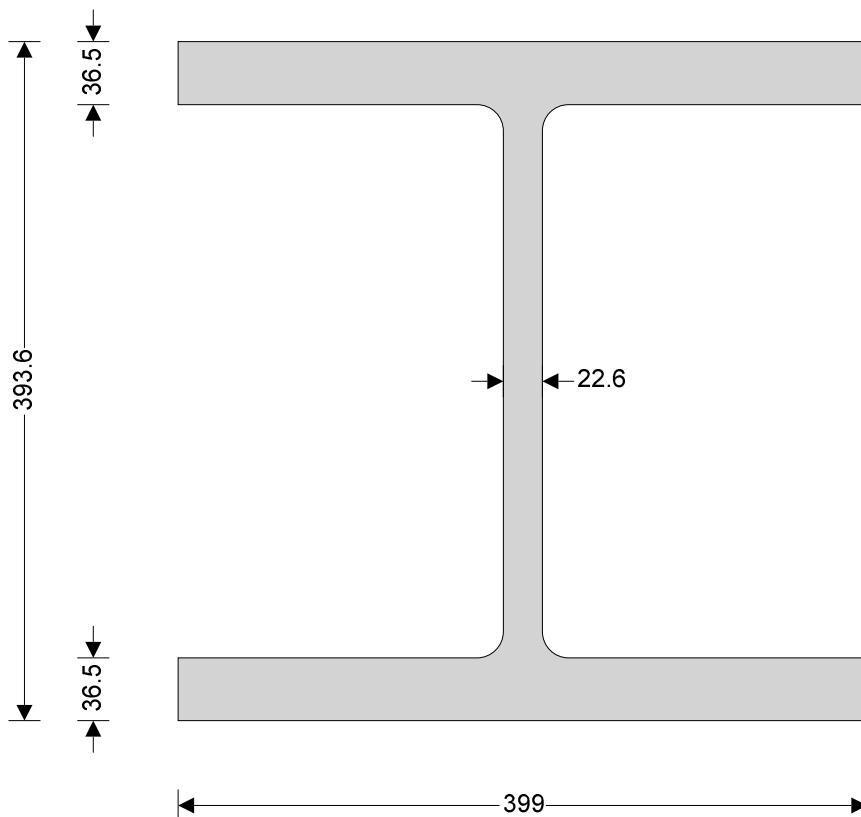
$f_y = 275$ N/mm²

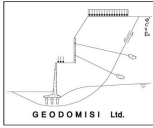
Nominal ultimate tensile strength;

$f_u = 430$ N/mm²

Modulus of elasticity;

$E = 210000$ N/mm²





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Partial factors - Section 6.1

Resistance of cross-sections; $\gamma_{M0} = 1.00$

Resistance of members to instability; $\gamma_{M1} = 1.00$

Resistance of tensile members to fracture; $\gamma_{M2} = 1.25$

Lateral restraint

Distance between major axis restraints; $L_y = 5000$ mm

Distance between minor axis restraints; $L_z = 5000$ mm

Effective length factors

Effective length factor in major axis; $K_y = 0.700$

Effective length factor in minor axis; $K_z = 1.000$

Effective length factor for torsion; $K_{LT} = 1.000$

Classification of cross sections - Section 5.5

$$\varepsilon = \sqrt{[235 \text{ N/mm}^2 / f_y]} = 0.92$$

Internal compression parts subject to bending and compression - Table 5.2 (sheet 1 of 3)

Width of section;

$$c = d = 290.2 \text{ mm}$$

$$\alpha = \min([h / 2 + N_{Ed} / (2 \times t_w \times f_y) - (t_f + r)] / c, 1) =$$

1.000

$$c / t_w = 13.9 \times \varepsilon \leq 396 \times \varepsilon / (13 \times \alpha - 1); \text{ Class 1}$$

Outstand flanges - Table 5.2 (sheet 2 of 3)

Width of section;

$$c = (b - t_w - 2 \times r) / 2 = 173 \text{ mm}$$

$$c / t_f = 5.1 \times \varepsilon \leq 9 \times \varepsilon;$$

Class 1

Section is class 1

Check shear - Section 6.2.6

Height of web;

$$h_w = h - 2 \times t_f = 320.6 \text{ mm}$$

Shear area factor;

$$\eta = 1.000$$

$$h_w / t_w < 72 \times \varepsilon / \eta$$

Shear buckling resistance can be ignored

Design shear force parallel to z axis;

$$V_{z,Ed} = 200 \text{ kN}$$

Shear area - cl 6.2.6(3);

$$A_v = \max(A - 2 \times b \times t_f + (t_w + 2 \times r) \times t_f, \eta \times h_w \times t_w)$$

$$= 9378 \text{ mm}^2$$

Design shear resistance - cl 6.2.6(2);

$$V_{c,z,Rd} = V_{pl,z,Rd} = A_v \times (f_y / \sqrt{3}) / \gamma_{M0} = 1489 \text{ kN}$$

PASS - Design shear resistance exceeds design shear force

Design shear force parallel to y axis;

$$V_{y,Ed} = 30 \text{ kN}$$

Shear area - cl 6.2.6(3);

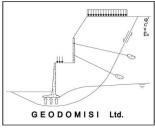
$$A_v = \max(2 \times b \times t_f - (t_w + 2 \times r) \times t_f, A - (h_w \times t_w)) =$$

$$29325 \text{ mm}^2$$

Design shear resistance - cl 6.2.6(2);

$$V_{c,y,Rd} = V_{pl,y,Rd} = A_v \times (f_y / \sqrt{3}) / \gamma_{M0} = 4656 \text{ kN}$$

PASS - Design shear resistance exceeds design shear force

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Check bending moment major (y-y) axis - Section 6.2.5

Design bending moment; $M_{y,Ed} = 450$ kNm
Design bending resistance moment - eq 6.13; $M_{c,y,Rd} = M_{pl,y,Rd} = W_{pl,y} \times f_y / \gamma_{M0} = 1598.4$ kNm

Slenderness ratio for lateral torsional buckling

Correction factor - Table 6.6; $k_c = 0.603$
 $C_1 = 1 / k_c^2 = 2.75$
Curvature factor; $g = \sqrt{[1 - (I_z / I_y)]} = 0.783$
Poissons ratio; $\nu = 0.3$
Shear modulus; $G = E / [2 \times (1 + \nu)] = 80769$ N/mm²
Unrestrained length; $L = 1.00 \times L_z = 5000$ mm
Elastic critical buckling moment;
 $M_{cr} = C_1 \times \pi^2 \times E \times I_z / (L^2 \times g) \times \sqrt{[I_w / I_z + L^2 \times G \times I_t / (\pi^2 \times E \times I_z)]} = 29413.9$ kNm
Slenderness ratio for lateral torsional buckling; $\bar{\lambda}_{LT} = \sqrt{[W_{pl,y} \times f_y / M_{cr}]} = 0.233$
Limiting slenderness ratio; $\bar{\lambda}_{LT,0} = 0.4$
 $\bar{\lambda}_{LT} < \bar{\lambda}_{LT,0}$ - Lateral torsional buckling can be ignored

Design resistance for buckling - Section 6.3.2.1

Buckling curve - Table 6.5; b
Imperfection factor - Table 6.3; $\alpha_{LT} = 0.34$
Correction factor for rolled sections; $\beta = 0.75$
LTB reduction determination factor;
 $\phi_{LT} = 0.5 \times [1 + \alpha_{LT} \times (\bar{\lambda}_{LT} - \bar{\lambda}_{LT,0}) + \beta \times \bar{\lambda}_{LT}^2] = 0.492$
LTB reduction factor - eq 6.57;
 $\chi_{LT} = \min(1 / [\phi_{LT} + \sqrt{(\phi_{LT}^2 - \beta \times \bar{\lambda}_{LT}^2)}], 1, 1 / \bar{\lambda}_{LT}^2) = 1.000$
Modification factor;
 $f = \min(1 - 0.5 \times (1 - k_c) \times [1 - 2 \times (\bar{\lambda}_{LT} - 0.8)^2], 1) = 0.929$
Modified LTB reduction factor - eq 6.58;
 $\chi_{LT,mod} = \min(\chi_{LT} / f, 1) = 1.000$
Design buckling resistance moment - eq 6.55; $M_{b,Rd} = \chi_{LT,mod} \times W_{pl,y} \times f_y / \gamma_{M1} = 1598.4$ kNm

PASS - Design buckling resistance moment exceeds design bending moment

Check bending moment minor (z-z) axis - Section 6.2.5

Design bending moment; $M_{z,Ed} = 125$ kNm
Design bending resistance moment - eq 6.13; $M_{c,z,Rd} = M_{pl,z,Rd} = W_{pl,z} \times f_y / \gamma_{M0} = 811$ kNm

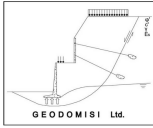
PASS - Design bending resistance moment exceeds design bending moment

Check compression - Section 6.2.4

Design compression force; $N_{Ed} = 4500$ kN
Design resistance of section - eq 6.10; $N_{c,Rd} = N_{pl,Rd} = A \times f_y / \gamma_{M0} = 10057$ kN

Slenderness ratio for major (y-y) axis buckling

Critical buckling length; $L_{cr,y} = L_y \times K_y = 3500$ mm
Critical buckling force; $N_{cr,y} = \pi^2 \times E_{SEC3} \times I_y / L_{cr,y}^2 = 168981.8$ kN



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Slenderness ratio for buckling - eq 6.50;

$$\bar{\lambda}_y = \sqrt{[A \times f_y / N_{cr,y}] = \mathbf{0.244}$$

Design resistance for buckling - Section 6.3.1.1

Buckling curve - Table 6.2;

b

Imperfection factor - Table 6.1;

$$\alpha_y = \mathbf{0.34}$$

Buckling reduction determination factor;

$$\phi_y = 0.5 \times [1 + \alpha_y \times (\bar{\lambda}_y - 0.2) + \bar{\lambda}_y^2] = \mathbf{0.537}$$

Buckling reduction factor - eq 6.49;

$$\chi_y = \min(1 / [\phi_y + \sqrt{(\phi_y^2 - \bar{\lambda}_y^2)}], 1) = \mathbf{0.984}$$

Design buckling resistance - eq 6.47;

$$N_{b,y,Rd} = \chi_y \times A \times f_y / \gamma_{M1} = \mathbf{9899.8 \text{ kN}}$$

PASS - Design buckling resistance exceeds design compression force

Slenderness ratio for minor (z-z) axis buckling

Critical buckling length;

$$L_{cr,z} = L_z \times K_z = \mathbf{5000 \text{ mm}}$$

Critical buckling force;

$$N_{cr,z} = \pi^2 \times E_{SEC3} \times I_z / L_{cr,z}^2 = \mathbf{32065.3 \text{ kN}}$$

Slenderness ratio for buckling - eq 6.50;

$$\bar{\lambda}_z = \sqrt{[A \times f_y / N_{cr,z}] = \mathbf{0.560}$$

Design resistance for buckling - Section 6.3.1.1

Buckling curve - Table 6.2;

c

Imperfection factor - Table 6.1;

$$\alpha_z = \mathbf{0.49}$$

Buckling reduction determination factor;

$$\phi_z = 0.5 \times [1 + \alpha_z \times (\bar{\lambda}_z - 0.2) + \bar{\lambda}_z^2] = \mathbf{0.745}$$

Buckling reduction factor - eq 6.49;

$$\chi_z = \min(1 / [\phi_z + \sqrt{(\phi_z^2 - \bar{\lambda}_z^2)}], 1) = \mathbf{0.809}$$

Design buckling resistance - eq 6.47;

$$N_{b,z,Rd} = \chi_z \times A \times f_y / \gamma_{M1} = \mathbf{8134.2 \text{ kN}}$$

PASS - Design buckling resistance exceeds design compression force

Check torsional and torsional-flexural buckling - Section 6.3.1.4

Torsional buckling length factor;

$$K_T = \mathbf{1.00}$$

Torsional buckling length;

$$L_{cr,T} = \max(L_y, L_z) \times K_T = \mathbf{5000 \text{ mm}}$$

Distance from shear centre to centroid in y axis;

$$y_0 = \mathbf{0.0 \text{ mm}}$$

Distance from shear centre to centroid in z axis;

$$z_0 = \mathbf{0.0 \text{ mm}}$$

Radius of gyration;

$$i_0 = \sqrt{[i_y^2 + i_z^2]} = \mathbf{194.6 \text{ mm}}$$

Elastic critical torsional buckling force;

$$N_{cr,T} = 1 / i_0^2 \times [G \times I_t + \pi^2 \times E_{SEC3} \times I_w / L_{cr,T}^2] =$$

57695.2 kN

Torsion factor;

$$\beta_T = 1 - (y_0 / i_0)^2 = \mathbf{1.000}$$

Elastic critical torsional-flexural buckling force

$$N_{cr,TF} = N_{cr,y} / (2 \times \beta_T) \times [1 + N_{cr,T} / N_{cr,y} - \sqrt{[(1 - N_{cr,T} / N_{cr,y})^2 + 4 \times (y_0 / i_0)^2 \times N_{cr,T} / N_{cr,y}]}] = \mathbf{57695.2 \text{ kN}}$$

Elastic critical buckling force;

$$N_{cr} = \min(N_{cr,T}, N_{cr,TF}) = \mathbf{57695.2 \text{ kN}}$$

Slenderness ratio for torsional buckling - eq 6.52;

$$\bar{\lambda}_T = \sqrt{[A \times f_y / N_{cr}] = \mathbf{0.418}$$

Design resistance for buckling - Section 6.3.1.1

Buckling curve - Table 6.2;

c

Imperfection factor - Table 6.1;

$$\alpha_T = \mathbf{0.49}$$

Buckling reduction determination factor;

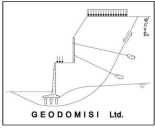
$$\phi_T = 0.5 \times [1 + \alpha_T \times (\bar{\lambda}_T - 0.2) + \bar{\lambda}_T^2] = \mathbf{0.640}$$

Buckling reduction factor - eq 6.49;

$$\chi_T = \min(1 / [\phi_T + \sqrt{(\phi_T^2 - \bar{\lambda}_T^2)}], 1) = \mathbf{0.888}$$

Design buckling resistance - eq 6.47;

$$N_{b,T,Rd} = \chi_T \times A \times f_y / \gamma_{M1} = \mathbf{8930.8 \text{ kN}}$$

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PASS - Design buckling resistance exceeds design compression force

Combined bending and axial force - Section 6.2.9

Normal force to plastic resistance force ratio;	$n = N_{Ed} / N_{pl,Rd} = \mathbf{0.45}$
Web area to gross area ratio;	$a_w = \min((A - 2 \times b \times t_f) / A, 0.5) = \mathbf{0.20}$
Design plastic moment resistance (y-y) - eq 6.13;	$M_{pl,y,Rd} = W_{pl,y} \times f_y / \gamma_{M0} = \mathbf{1598.4 \text{ kNm}}$
Reduced plastic mnt resistance (y-y)- eq 6.36;	$M_{N,y,Rd} = M_{pl,y,Rd} \times \min((1 - n) / (1 - 0.5 \times a_w), 1) = \mathbf{983.3 \text{ kNm}}$
Design plastic moment resistance (z-z) - eq 6.13;	$M_{pl,z,Rd} = W_{pl,z} \times f_y / \gamma_{M0} = \mathbf{811.0 \text{ kNm}}$
Reduced plastic mnt resistance (z-z) - eq 6.38;	$M_{N,z,Rd} = M_{pl,z,Rd} \times (1 - ((n - a_w) / (1 - a_w))^2) = \mathbf{735.0 \text{ kNm}}$
Parameter introducing effect of biaxial bending;	$\alpha_{bi} = \mathbf{2.00}$
Parameter introducing effect of biaxial bending;	$\beta_{bi} = \max(5 \times n, 1) = \mathbf{2.24}$
Interaction formula – eq (6.41);	$(M_{y,Ed} / M_{N,y,Rd})^{\alpha_{bi}} + (M_{z,Ed} / M_{N,z,Rd})^{\beta_{bi}} = \mathbf{0.228}$

PASS - Reduced bending resistance moment exceeds design bending moment

Check combined bending and compression - Section 6.3.3

Equivalent uniform moment factors - Table B.3;	$C_{my} = \mathbf{0.400}$
	$C_{mz} = \mathbf{0.600}$
	$C_{mLT} = \mathbf{0.400}$

Interaction factors k_{ij} for members susceptible to torsional deformations - Table B.2

Characteristic moment resistance;	$M_{y,Rk} = W_{pl,y} \times f_y = \mathbf{1598.4 \text{ kNm}}$
Characteristic moment resistance;	$M_{z,Rk} = W_{pl,z} \times f_y = \mathbf{811 \text{ kNm}}$
Characteristic resistance to normal force;	$N_{Rk} = A \times f_y = \mathbf{10057 \text{ kN}}$
Interaction factors;	$k_{yy} = C_{my} \times [1 + \min(\bar{\lambda}_y - 0.2, 0.8) \times N_{Ed} / (\chi_y \times N_{Rk} / \gamma_{M1})] = \mathbf{0.408}$
	$k_{zy} = 1 - 0.1 \times \max(1, \bar{\lambda}_z) \times N_{Ed} / ((C_{mLT} - 0.25) \times \chi_z \times N_{Rk} / \gamma_{M1}) = \mathbf{0.631}$
	$k_{zz} = C_{mz} \times [1 + \min(2 \times \bar{\lambda}_z - 0.6, 1.4) \times N_{Ed} / (\chi_z \times N_{Rk} / \gamma_{M1})] = \mathbf{0.773}$
	$k_{yz} = 0.6 \times k_{zz} = \mathbf{0.464}$
Interaction formulae - eq 6.61 & eq 6.62;	$N_{Ed} / (\chi_y \times N_{Rk} / \gamma_{M1}) + k_{yy} \times M_{y,Ed} / (\chi_{LT} \times M_{y,Rk} / \gamma_{M1}) + k_{yz} \times M_{z,Ed} / (M_{z,Rk} / \gamma_{M1}) = \mathbf{0.641}$
	$N_{Ed} / (\chi_z \times N_{Rk} / \gamma_{M1}) + k_{zy} \times M_{y,Ed} / (\chi_{LT} \times M_{y,Rk} / \gamma_{M1}) + k_{zz} \times M_{z,Ed} / (M_{z,Rk} / \gamma_{M1}) = \mathbf{0.850}$

PASS - Combined bending and compression checks are satisfied