

Civil & Geotechnical Engineering Consulting Company for  
 Structural Engineering, Soil Mechanics, Rock Mechanics,  
 Foundation Engineering & Retaining Structures.  
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GEODOMISI Ltd. - Dr. Costas Sachpazis

## CANTILEVER RETAINING WALL DESIGN

GEOMETRY			APPLIED LOADS			
Conc. Stem Height .....	5.18	m	Uniform Surcharge .....	0.0	KPa	
Stem Thickness Top .....	30.5	cm	Strip Pressure .....	0.0	KPa	
Stem Thickness Bot .....	50.8	cm	<i>Strip 0.6 m deep, 1.2 m wide @ 0.9 m from Stem</i>			
Footing Thickness .....	50.8	cm	Stem Vertical (Dead) .....	0.0	KN/m	
Toe Length .....	1.22	m	Stem Vertical (Live) .....	0.0	KN/m	
Heel Length .....	1.52	m	Vertical Load Eccentricity .....	15.2	cm	
Soil Cover @ Toe .....	0.61	m	Wind Load on Stem .....	0.0	KPa	
Backfill Height .....	4.57	m	OK	Wind Height from Top .....	1.52	m
Backfill Slope Angle .....	10.0	deg				

### BACKFILL PROPERTIES

Wall taper  $\alpha = a \tan(\text{taper} / H) = a \tan((50.8 - 30.5) / 100 / 5.18) = 0.039 \text{ rad}$   
 Backfill slope  $\beta = \text{slope} * \pi / 180 = 10.0 * 3.14 / 180 = 0.175 \text{ rad}$   
 Internal friction  $\phi = \text{Int. friction} * \pi / 180 = 28.0 * 3.14 / 180 = 0.489 \text{ rad}$   
 Wall-soil friction  $\delta = \phi / 2 = 0.489 / 2 = 0.244 \text{ rad}$   
 Seismic angle  $\theta = a \tan(kh / (1 - kv)) = a \tan(0.00 / (1 - 0.00)) = 0.000 \text{ rad}$   
 Footing length  $ftg = \text{toe} + \text{stem} + \text{heel} = 1.22 + 50.8 / 100 + 1.52 = 3.25 \text{ m}$   
 Height for Stability  $H_s = \text{wedge} + \text{backfill} + \text{footing} = 0.30 + 4.57 + 50.8 / 100 = 5.38 \text{ m}$   
 Earth pressure theory = **Coulomb Active**    Moist density = **19 KN/m<sup>3</sup>**    Saturated density = **20 KN/m<sup>3</sup>**

$$\text{Active coefficient } ka = \frac{\cos^2(\phi + \alpha)}{\cos^2 \alpha * \cos(\delta + \alpha) * [1 + (\frac{\sin(\phi + \delta) * \sin(\phi - \beta)}{\cos(\delta + \alpha) * \cos(\beta - \alpha)})^{1/2}]^2} = 0.39$$

Active pressure  $pa = ka * \gamma = 0.39 * 18.8 = 7.4 \text{ KPa/m of height}$

**- For stability analysis (non-seismic)**

Active force  $Pa = ka * \gamma * H_s^2 / 2 = 0.39 * 18.8 * 5.38^2 / 2 = 107.0 \text{ KN/m}$

$Pa_h = Pa * \cos(\delta + \alpha) = 107.0 * \cos(0.244 + 0.039) = 102.7 \text{ KN/m}$

$Pa_v = Pa * \sin(\delta + \alpha) = 107.0 * \sin(0.244 + 0.039) = 29.9 \text{ KN/m}$

Water force  $P_w = (ka * (\gamma_s - \gamma_w - \gamma) + \gamma_w) * (\text{Water table})^2 / 2$

$$P_w = (0.39 * (20.4 - 9.8 - 18.8) + 9.8) * 1.52^2 / 2 = 7.6 \text{ KN/m}$$

**- For stem design (non-seismic)**

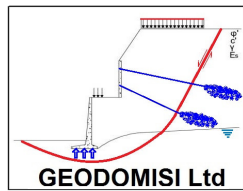
Active force  $Pa = ka * \gamma * H^2 / 2 = 0.39 * 18.8 * 4.57^2 / 2 = 77.3 \text{ KN/m}$

$Pa_h = Pa * \cos(\delta + \alpha) = 77.3 * \cos(0.244 + 0.039) = 74.2 \text{ KN/m}$

$Pa_v = Pa * \sin(\delta + \alpha) = 77.3 * \sin(0.244 + 0.039) = 21.6 \text{ KN/m}$

Water force  $P_w = (ka * (\gamma_s - \gamma_w - \gamma) + \gamma_w) * (\text{Water table} - Ftg)^2 / 2$

$$P_w = (0.39 * (20.4 - 9.8 - 18.8) + 9.8) * (1.52 - 50.8 / 100)^2 / 2 = 3.4 \text{ KN/m}$$



## CANTILEVER RETAINING WALL DESIGN

Hor. seismic coeff.  $k_h = 0.00$

Ver. seismic coeff.  $k_v = 0.00$

$$\text{Active seismic coeff. } k_{ae} = \frac{\cos^2(\phi - \alpha - \theta)}{\cos\theta * \cos^2\alpha * \cos(\delta + \alpha + \theta) * [1 + (\frac{\sin(\phi + \delta) * \sin(\phi - \beta - \theta)}{\cos(\delta + \alpha + \theta) * \cos(\beta - \alpha)})^{1/2}]^2} = 0.39$$

- For stability analysis (seismic)

$$\text{Seismic force } P_{ae} = k_{ae} * \gamma * H_s^2 / 2 * (1 - k_v) = 0.39 * 18.8 * 5.38^2 / 2 * (1 - 0.0) = 107.0 \text{ KN/m}$$

$$P_{aeh} = P_{ae} * \cos(\delta + \alpha) = 107.0 * \cos(0.244 + 0.039) = 102.7 \text{ KN/m}$$

$$P_{aev} = P_{ae} * \sin(\delta + \alpha) = 107.0 * \sin(0.244 + 0.039) = 29.9 \text{ KN/m}$$

$$\text{Water force } P_{we} = k_h * (\gamma_s - \gamma) * (\text{water})^2 / 2$$

$$P_{we} = 0.00 * (20.4 - 18.8) * (1.52)^2 / 2 = 0.0 \text{ KN/m}$$

- For stem design (seismic)

$$\text{Seismic force } P_{ae} = k_{ae} * \gamma * H^2 / 2 = 0.39 * 18.8 * 4.57^2 / 2 = 77.3 \text{ KN/m}$$

$$P_{aeh} = P_{ae} * \cos(\delta + \alpha) = 77.3 * \cos(0.244 + 0.039) = 74.2 \text{ KN/m}$$

$$P_{aev} = P_{ae} * \sin(\delta + \alpha) = 77.3 * \sin(0.244 + 0.039) = 21.6 \text{ KN/m}$$

$$\text{Water force } P_{we} = k_h * (\gamma_s - \gamma) * (\text{water table} - \text{ftg})^2 / 2$$

$$P_{we} = 0.00 * (20.4 - 18.8) * (1.52 - 50.8 / 100)^2 / 2 = 0.0 \text{ KN/m}$$

### OVERTURNING CALCULATIONS (Comb. D+H+W)

- Overturning Forces

$$\text{Backfill} = \text{Lat factor} * P_{ah} = 1.0 * 102.7 = 102.7 \text{ KN/m}$$

$$\text{Arm} = H_s / 3 = 5.38 / 3 = 1.79 \text{ m}$$

$$\text{Moment} = 102.7 * 1.79 = 184.1 \text{ KN-m/m}$$

$$\text{Water table} = \text{Lat factor} * P_w = 1.0 * 7.6 = 7.6 \text{ KN/m}$$

$$\text{Arm} = \text{Water table} / 3 = 1.52 / 3 = 0.51 \text{ m}$$

$$\text{Moment} = 7.6 * 0.51 = 3.9 \text{ KN-m/m}$$

$$\text{Surcharge} = \text{Lat factor} * k_a * \text{Surcharge} * H_s = 1.0 * 0.38 * 0.0 * 5.38 = 0.0 \text{ KN/m}$$

$$\text{Arm} = H_s / 2 = 5.38 / 2 = 2.69 \text{ m}$$

$$\text{Moment} = 0.0 * 2.69 = 0.0 \text{ KN-m/m}$$

$$\text{Strip load} = \sum \text{Lat factor} * 2 * Q / n * [\beta - \sin\beta * \cos(2\alpha)] = 0.0 \text{ KN/m}$$

$$\text{Arm} = 2.29 \text{ m}$$

$$\text{Moment} = 0.0 * 2.29 = 0.0 \text{ KN-m/m}$$

$$\text{Wind load} = \text{WL factor} * \text{Pressure} * \text{Wind height} = 1.0 * 0.0 * 1.52 = 0.0 \text{ KN/m}$$

$$\text{Arm} = \text{Ftg} + \text{Stem} - \text{Wind height} / 2 = 50.8 / 100 + 5.18 - 1.52 / 2 = 4.93 \text{ m}$$

$$\text{Moment} = 0.0 * 4.93 = 0.0 \text{ KN-m/m}$$

$$\text{Backfill seismic} = \text{EQ factor} * (P_{aeh} - P_{ah}) = 0.0 * (102.7 - 102.7) = 0.0 \text{ KN/m}$$

$$\text{Arm} = 0.6 * H_s = 0.6 * 5.38 = 3.23 \text{ m}$$

$$\text{Moment} = 0.0 * 3.23 = 0.0 \text{ KN-m/m}$$

$$\text{Water seismic} = \text{EQ factor} * P_{we} = 0.0 * 0.0 = 0.0 \text{ KN/m}$$

$$\text{Arm} = \text{Water table} / 3 = 1.52 / 3 = 0.51 \text{ m}$$

$$\text{Moment} = 0.0 * 0.51 = 0.0 \text{ KN-m/m}$$

*Wall selfweight seismic effect not considered in calculations*

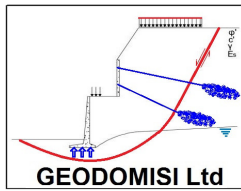
Wall seismic = 0 KN

Moment = 0 KN-m/m

$$\text{Hor. resultant } R_h = 102.7 + 7.6 + 0.0 + 0.0 + 0.0 + 0.0 + 0.0 + 0.0 = 110.3 \text{ KN/m}$$

$$\text{Overturning moment } OTM = 184.1 + 3.9 + 0.0 + 0.0 + 0.0 + 0.0 + 0.0 + 0.0 = 188.0 \text{ KN-m/m}$$

$$\text{Arm of hor. resultant} = OTM / R_h = 188.0 / 110.3 = 1.70 \text{ m}$$



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## CANTILEVER RETAINING WALL DESIGN

### - Resisting Forces

Stem weight  $W_{Stem} = DL \text{ factor} * Thickness * Height * \gamma_c = 4.0 * 30.5 / 100 * 5.18 * 24.00 = 37.9 \text{ KN/m}$

Arm =  $Toe + Thickness / 2 = 1.22 + 30.5 / 100 / 2 = 1.37 \text{ m}$                       Moment =  $37.9 * 1.37 = 52.0 \text{ KN-m/m}$

Stem taper  $W_{Taper} = DL \text{ factor} * \Delta Thick * Height / 2 * \gamma_c = 1.0 * (50.8 - 30.5) / 100 * 5.18 / 2 * 24.00 = 12.6 \text{ KN/m}$

Arm =  $Toe + Thick + \Delta Thick * 2 / 3 = 1.22 + 30.5 / 100 - (50.8 - 30.5) / 100 * 2 / 3 = 1.59 \text{ m}$

Moment =  $12.6 * 1.59 = 20.1 \text{ KN-m/m}$

CMU stem at top =  $0.0 \text{ KN/m}$

Arm =  $Toe + Thickness / 2 = 1.22 + 0.0 / 100 / 2 = 0.00 \text{ m}$

Moment =  $0.0 * 0.00 = 0.0 \text{ KN-m/m}$

Ftg. weight  $W_{Ftg} = DL \text{ factor} * Length * Thickness * \gamma_c = 1.0 * 3.25 * 50.8 / 100 * 24.00 = 39.6 \text{ KN/m}$

Arm =  $Length / 2 = 3.25 / 2 = 1.62 \text{ m}$                       Moment =  $39.6 * 1.62 = 64.3 \text{ KN-m/m}$

Key weight  $W_{Key} = DL \text{ factor} * Depth * Thickness * \gamma_c = 1.0 * 30.50 / 100 * 30.5 / 100 * 24.00 = 2.2 \text{ KN/m}$

Arm =  $Toe + Thickness / 2 = 1.22 + 30.5 / 100 / 2 = 1.37 \text{ m}$                       Moment =  $2.2 * 1.37 = 3.1 \text{ KN-m/m}$

Soil cover =  $DL \text{ factor} * Toe * Soil \text{ cover} * \gamma = 1.0 * 1.22 * 0.61 * 18.8 = 14.0 \text{ KN/m}$

Arm =  $Toe / 2 = 1.22 / 2 = 0.61 \text{ m}$                       Moment =  $14.0 * 0.61 = 8.5 \text{ KN-m/m}$

Stem wedge =  $DL \text{ factor} * \Delta Thick * Height / 2 * \gamma = 1.0 * (50.8 - 30.5) / 100 * 4.57 / 2 * 18.8 = 8.7 \text{ KN/m}$

Arm =  $Toe + Thick - \Delta Thick / 3 = 1.22 + 50.8 / 100 - (50.8 - 30.5) / 100 / 3 = 1.66 \text{ m}$

Moment =  $8.7 * 1.66 = 14.5 \text{ KN-m/m}$

Backfill weight =  $DL \text{ factor} * Heel * Height * \gamma = 1.0 * 1.52 * 4.57 * 18.8 = 130.6 \text{ KN/m}$

Arm =  $Ftg - Heel / 2 = 3.25 - 1.52 / 2 = 2.49 \text{ m}$                       Moment =  $130.6 * 2.49 = 324.9 \text{ KN-m/m}$

Backfill slope =  $DL \text{ factor} * (Heel + \Delta Thick) * Wedge / 2 * \gamma =$

$= 1.0 * (1.5 + (50.8 - 30.5) / 100) * 0.30 / 2 * 18.8 = 4.9 \text{ KN/m}$

Arm =  $ftg - (Heel + \Delta Thick) / 3 = 3.25 - (1.52 + (50.8 - 30.5) / 100) / 3 = 2.67 \text{ m}$

Moment =  $4.9 * 2.67 = 13.0 \text{ KN-m/m}$

Water =  $DL \text{ factor} * Heel * (Water - Ftg) * (\gamma_s - \gamma) = 1.0 * 1.52 * (1.52 - 50.8 / 100) * (20.4 - 18.8) = 2.5 \text{ KN/m}$

Arm =  $Ftg - Heel / 2 = 3.25 - 1.52 / 2 = 2.49 \text{ m}$                       Moment =  $2.5 * 2.49 = 6.1 \text{ KN-m/m}$

Seismic Pae-Pa =  $EQ \text{ factor} * (Paev - Pav) = 0.0 * (29.9 - 29.9) = 0.0 \text{ KN/m}$

Arm =  $Footing \text{ length} = 3.25 \text{ m}$                       Moment =  $0.0 * 3.25 = 0.0 \text{ KN-m/m}$

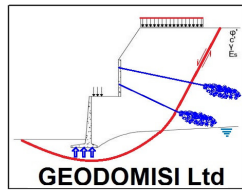
Backfill Pav =  $Lat \text{ factor} * Pav = 1.0 * 29.9 = 29.9 \text{ KN/m}$

Arm =  $Footing \text{ length} = 3.25 \text{ m}$                       Moment =  $29.9 * 3.25 = 97.2 \text{ KN-m/m}$

Concentrated =  $DL \text{ factor} * Ver \text{ load} + LL \text{ factor} * Ver \text{ load} = 1.0 * 0.0 + 0.0 * 0.0 = 0.0 \text{ KN/m}$

Arm =  $Toe + Stem - Ecc = 1.22 + (30.5 - 15.2) / 100 = 1.37 \text{ m}$

Moment =  $0.0 * 1.37 = 0.0 \text{ KN-m/m}$



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## CANTILEVER RETAINING WALL DESIGN

$$\text{Surcharge} = \text{Srch factor} * (\text{Heel} + \Delta\text{Thick}) * \text{Surcharge} = 1.0 * (1.5 + (50.8 - 30.5) / 100) * 0.0 = 0.0 \text{ KN/m}$$

$$\text{Arm} = \text{ftg} - (\text{Heel} + \Delta\text{Thick}) / 2 = 3.25 - (1.52 + (50.8 - 30.5) / 100) / 2 = 2.39 \text{ m}$$

$$\text{Moment} = 0.0 * 2.39 = 0.0 \text{ KN-m/m}$$

$$\text{Strip} = \text{Strip factor} * \text{Surcharge} * \text{Heel} = 1.0 * 0.0 * 1.52 = 0.0 \text{ KN/m}$$

$$\text{Arm} = \text{Footing} - \text{Heel} / 2 = 3.25 - 1.52 / 2 = 2.49 \text{ m} \quad \text{Moment} = 0.0 * 2.49 = 0.0 \text{ KN-m/m}$$

$$\text{Buoyancy} = \text{DL factor} * \gamma_w * \text{Water table} * \text{Ftg} = 1.0 * 9.8 * 1.52 * 3.25 = -48.4 \text{ KN/m}$$

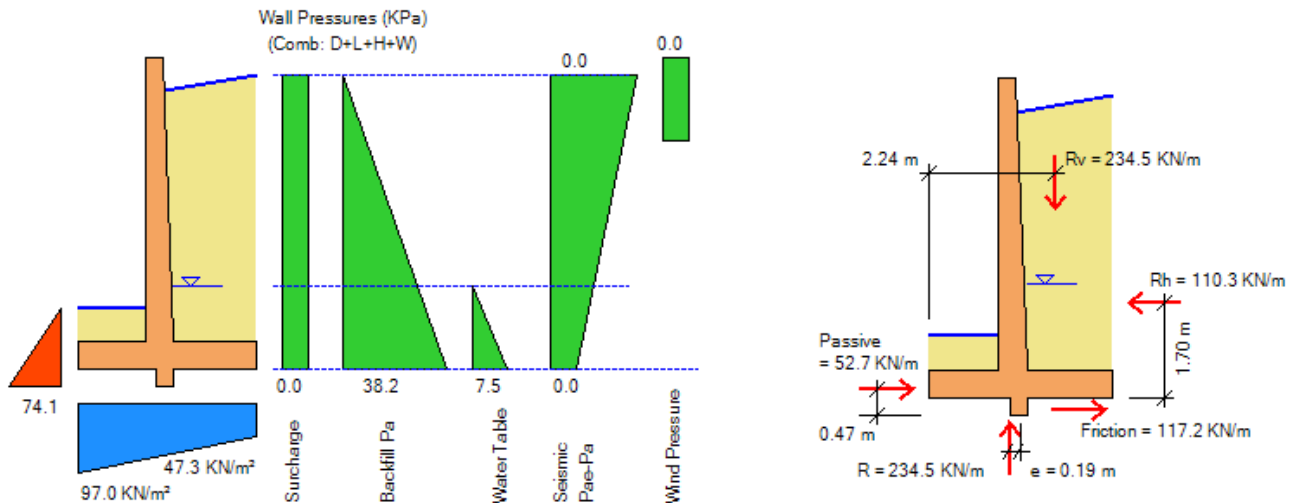
$$\text{Arm} = \text{Footing} / 2 = 3.25 / 2 = 1.62 \text{ m} \quad \text{Moment} = -48.4 * 1.62 = -78.7 \text{ KN-m/m}$$

$$\text{Ver. resultant } R_v = \Sigma \text{ Vertical forces} = 234.5 \text{ KN/m}$$

$$\text{Resisting moment } RM = \Sigma \text{ Moments} = 525.1 \text{ KN-m/m}$$

$$\text{Arm of ver. resultant} = RM / R_v = 525.1 / 234.5 = 2.24 \text{ m}$$

$$\text{Overturning ratio} = RM / OTM = 525.1 / 188.0 = 2.79 > 1.50 \quad \text{OK}$$



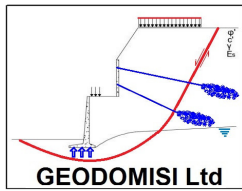
### SOIL BEARING PRESSURES (Comb. D+H+W)

$$\text{Eccentricity} = \frac{Ftg}{2} - \frac{RM - OTM}{R_v} = \frac{3.25}{2} - \frac{525.1 - 188.0}{234.5} = 0.19 \text{ m}$$

$$\text{Bearing length} = \text{Min} (Ftg, 3 * (Ftg / 2 - Ecc)) = \text{Min} (3.25, 3 * (3.25 / 2 - 0.19)) = 3.25 \text{ m}$$

$$\text{Toe bearing} = \frac{R_v}{Ftg} + \frac{6 * R_v * Ecc}{Ftg^2} = \frac{234.5}{3.25} + \frac{6 * 234.5 * 0.19}{3.25^2} = 97.0 \text{ KN/m}^2 < 191.6 \text{ KN/m}^2 \text{ OK}$$

$$\text{Heel bearing} = \frac{R_v}{Ftg} - \frac{6 * R_v * Ecc}{Ftg^2} = \frac{234.5}{3.25} - \frac{6 * 234.5 * 0.19}{3.25^2} = 47.3 \text{ KN/m}^2$$



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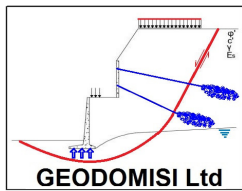
## CANTILEVER RETAINING WALL DESIGN

### SLIDING CALCULATIONS (Comb. D+H+W)

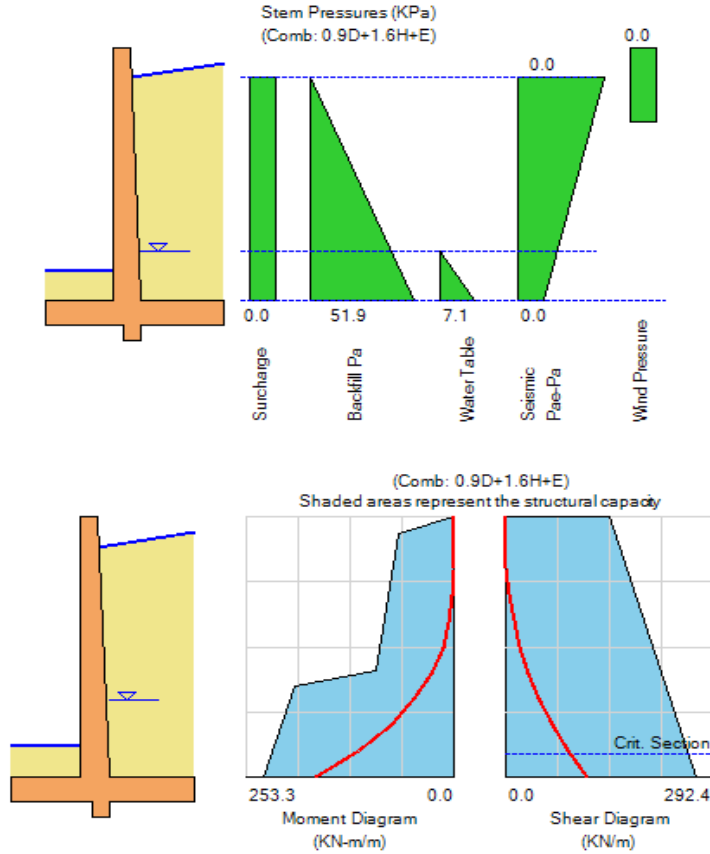
Passive coefficient  $kp = 1 / ka = 1 / 0.36 = 2.77 \text{ KN/m}^2$   
 Passive depth  $Dp = \text{Soil cover} + Ftg + \text{Key} - \text{Neglect depth} = 0.61 + (50.8 + 30.5) / 100 - 0.00 = 1.42 \text{ m}$   
 Passive pressure top  $= kp * \gamma * \text{Neglect depth} = 2.77 * 18.8 * 0.00 = 0.00 \text{ KN/m}^2$   
 Passive pressure bot  $= kp * \gamma * (Dp + \text{Neglect depth}) = 2.77 * 18.8 * (1.42 + 0.00) = 74.10 \text{ KN/m}^2$   
 Passive force  $= (\text{Pressure top} + \text{Pressure bot}) / 2 * Dp = (0.00 + 74.10) / 2 * 1.42 = 52.7 \text{ KN/m}$   
 Friction force  $= \text{Max}(0, Rv * \text{Friction coeff.}) = \text{Max}(0, 234.5 * 0.50) = 117.2 \text{ KN/m}$   
 Sliding ratio  $= (\text{Passive} + \text{Friction}) / Rh = (52.7 + 117.2) / 110.3 = 1.54 > 1.50 \text{ OK}$

### STEM DESIGN (Comb. 0.9D+1.6H+E)

Backfill  $= \text{Lat factor} * Pah = 1.6 * 73.7 = 118.7 \text{ KN/m}$   
 Arm  $= Hb / 3 = 4.57 / 3 = 1.52 \text{ m}$  Moment  $= 118.7 * 1.52 = 180.8 \text{ KN-m/m}$   
 Water table  $= \text{Lat factor} * Pw = 1.6 * 3.3 = 5.4 \text{ KN/m}$   
 Arm  $= (\text{Water table} - Ftg) / 3 = (1.52 - 50.8 / 100) / 3 = 0.34 \text{ m}$  Moment  $= 5.4 * 0.34 = 2.7 \text{ KN-m/m}$   
 Surcharge  $= \text{Lat factor} * ka * \text{Surcharge} * Hb = 1.6 * 0.38 * 0.0 * 4.57 = 0.0 \text{ KN/m}$   
 Arm  $= Hb / 2 = 4.57 / 2 = 2.29 \text{ m}$  Moment  $= 0.0 * 2.29 = 0.0 \text{ KN-m/m}$   
 Strip load  $= \Sigma \text{Lat factor} * 2 * Q / n * [\beta - \text{Sin } \beta * \text{Cos}(2\alpha)] = 0.0 \text{ KN/m}$   
 Arm  $= 2.29 \text{ m}$  Moment  $= 0.0 * 2.29 = 0.0 \text{ KN-m/m}$   
 Wind load  $= \text{WL factor} * \text{Pressure} * \text{Wind height} = 0.0 * 0.0 * 1.52 = 0.0 \text{ KN/m}$   
 Arm  $= \text{Stem} - \text{Wind height} / 2 = 5.18 - 1.52 / 2 = 4.42 \text{ m}$  Moment  $= 0.0 * 4.42 = 0.0 \text{ KN-m/m}$   
 Backfill seismic  $= \text{EQ factor} * (Paeh - Pah) = 1.0 * (74.2 - 74.2) = 0.0 \text{ KN/m}$   
 Arm  $= 0.6 * Hb = 0.6 * 4.57 = 2.74 \text{ m}$  Moment  $= 0.0 * 2.74 = 0.0 \text{ KN-m/m}$   
 Water seismic  $= \text{EQ factor} * Pwe = 1.0 * 0.0 = 0.0 \text{ KN/m}$   
 Arm  $= (\text{Water table} - Ftg) / 3 = (1.52 - 50.8 / 100) / 3 = 0.34 \text{ m}$  Moment  $= 0.0 * 0.34 = 0.0 \text{ KN-m/m}$   
 Max. shear  $= 118.7 + 5.4 + 0.0 + 0.0 + 0.0 + 0.0 + 0.0 = 124.1 \text{ KN/m}$   
 Shear at critical section  $= \text{Max shear} - \text{Max shear} / Hb * d = 124.1 - 124.1 / 4.57 * 42.9 / 100 = 112.4 \text{ KN/m}$   
 Max. moment  $= 180.8 + 2.7 + 0.0 + 0.0 + 0.0 + 0.0 + 0.0 = 183.6 \text{ KN-m/m}$   
 Shear strength  $\phi Vn = \phi * 0.17 * (fc)^{1/2} * 10 * d$  ACI Eq. (11-3)  
 $\phi Vn = 0.75 * 0.17 * (28)^{1/2} * 10 * 42.9 = 280.9 \text{ KN/m} > 112.4 \text{ KN/m OK}$   
 Use D20 @ 20.0 cm  $As = 15.71 \text{ cm}^2/\text{m}$   $\rho = As / bd = 15.71 / (100 * 44.7) = 0.0035$   
 Bending strength  $\phi Mn = \phi * d^2 * fc * q * (1 - 0.59 * q)$  ACI 10.2.7  
 $\phi Mn = 0.90 * 44.7^2 * 27.6 * 0.053 * (1 - 0.59 * 0.053) = 253.3 \text{ KN-m/m} > 183.6 \text{ KN-m/m OK}$   
 Hooked  $Ldh = 0.24 * fy / (fc)^{1/2} * db * 0.7 = 0.24 * 413.7 / (27.6)^{1/2} * 2.00 * 0.7 * 0.72 = 19.2 \text{ cm}$  ACI 12.5  
 Dev. length at footing  $= Ftg - \text{Cover} = 50.8 - 7.6 = 43.2 \text{ cm} > 19.2 \text{ cm OK}$   
 $As \text{ min} = \text{Min}(\text{Max}((1.4 / fy, 0.25 * \sqrt{fc} / fy) * b * d), 1.33 * As \text{ req})$  ACI 10.5  
 $= \text{Min}(\text{Max}((1.4 / 414, 0.25 * (27.6)^{1/2} / 414) * 100 * 44.7, 1.33 * 11.3) = 15.0 \text{ cm}^2/\text{m}$   
 Min. steel area ratio  $= As \text{ min} / As = 15.04 / 15.71 = 0.96 < 1.0 \text{ OK}$



## CANTILEVER RETAINING WALL DESIGN



### HEEL DESIGN (Comb. 1.4D)

Bearing force = 0.0 KN/m (Neglect bearing pressure for heel design)

$$\text{Arm} = (\text{Bearing1} * \text{Heel}^2 / 2 + (\text{Bearing2} - \text{Bearing1}) * \text{Heel}^2 / 6) / \text{Force}$$

$$= (164.4 * 1.52^2 / 2 + (93.0 - 164.4) * 1.52^2 / 6) / 0.0 = 0.83 \text{ m}$$

$$\text{Moment} = 0.0 * 0.83 = 0.0 \text{ KN-m/m}$$

$$\text{Concrete weight} = \text{DL factor} * \text{Thick} * \text{Heel} * \gamma_c = 1.4 * 50.8 / 100 * 1.52 * 24.00 = 25.9 \text{ KN/m}$$

$$\text{Arm} = \text{Heel} / 2 = 1.52 / 2 = 0.76 \text{ m} \quad \text{Moment} = 25.9 * 0.76 = 19.7 \text{ KN-m/m}$$

$$\text{Backfill weight} = \text{DL factor} * \text{Heel} * \text{Height} * \gamma = 1.4 * 1.52 * 4.57 * 18.8 = 182.8 \text{ KN/m}$$

$$\text{Arm} = \text{Heel} / 2 = 1.52 / 2 = 0.76 \text{ m} \quad \text{Moment} = 182.8 * 0.76 = 139.0 \text{ KN-m/m}$$

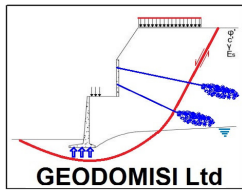
$$\text{Backfill slope} = \text{DL factor} * (\text{Heel} + \Delta \text{Thick}) * \text{Wedge} / 2 * \gamma =$$

$$= 1.4 * (1.5 + (50.8 - 30.5) / 100) * 0.30 / 2 * 18.8 = 6.8 \text{ KN/m}$$

$$\text{Arm} = \text{Heel} * 2 / 3 = 1.52 * 2 / 3 = 1.01 \text{ m} \quad \text{Moment} = 6.8 * 1.01 = 6.9 \text{ KN-m/m}$$

$$\text{Water} = \text{DL factor} * \text{Heel} * \text{Water table} * (\gamma_s - \gamma) = 1.4 * 1.52 * 1.52 * (20.4 - 18.8) = 3.4 \text{ KN/m}$$

$$\text{Arm} = \text{Heel} / 2 = 1.52 / 2 = 0.76 \text{ m} \quad \text{Moment} = 3.4 * 0.76 = 2.6 \text{ KN-m/m}$$



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## CANTILEVER RETAINING WALL DESIGN

$$\text{Surcharge} = \text{Srch factor} * (\text{Heel} + \Delta \text{Thick}) * \text{Surcharge} = 1.4 * (1.5 + (50.8 - 30.5) / 100) * 0.0 = 0.0 \text{ KN/m}$$

$$\text{Arm} = \text{Heel} / 2 = 1.52 / 2 = 0.76 \text{ m}$$

$$\text{Moment} = 0.0 * 0.76 = 0.0 \text{ KN-m/m}$$

$$\text{Strip} = \text{Strip factor} * \text{Surcharge} * \text{Width} = 1.4 * 0.0 * 1.22 = 0.0 \text{ KN/m}$$

$$\text{Arm} = \text{Distance} - \Delta \text{Stem} + \text{Width} / 2 = 0.91 - (50.8 - 30.5) / 100 + 1.22 / 2 = 0.76 \text{ m}$$

$$\text{Moment} = 0.0 * 0.76 = 0.0 \text{ KN-m/m}$$

$$\text{Max. Shear } V_u = -0.0 + 25.9 + 182.8 + 6.8 + 3.4 + 0.0 + 0.0 = 219.0 \text{ KN/m}$$

$$\text{Max. Moment } M_u = -0.0 + 19.7 + 139.0 + 6.9 + 2.6 + 0.0 + 0.0 = 168.2 \text{ KN/m}$$

$$\text{Shear strength } \phi V_n = \phi * 0.17 * (f_c)^{1/2} * 10 * d$$

ACI Eq. (11-3)

$$\phi V_n = 0.75 * 0.17 * (28)^{1/2} * 10 * 44.7 = 292.4 \text{ KN/m} > V_u = 219.0 \text{ KN/m OK}$$

$$\text{Use D20 @ 20.0 cm} \quad A_s = 15.71 \text{ cm}^2/\text{m} \quad \rho = A_s / b d = 15.71 / (100 * 44.7) = 0.0035$$

$$\text{Bending strength } \phi M_n = \phi * d^2 * f_c * q * (1 - 0.59 * q)$$

ACI 10.2.7

$$\phi M_n = 0.90 * 44.7^2 * 27.6 * 0.053 * (1 - 0.59 * 0.053) = 253.3 \text{ KN-m/m} > M_u = 168.2 \text{ KN-m/m OK}$$

$$\text{Cover factor} = \text{Min} (2.5, (\text{Cover} + db / 2, \text{Spacing} / 2) / db) = \text{Min} (2.5, (5.1 + 2.00 / 2, 20.0 / 2) / 2.00) = 2.5$$

$$\text{Straight } L_d = f_y / 1.1 / (f_c)^{1/2} * \text{Size} * \text{Location} / \text{Cover} * db$$

ACI Eq. (12-1)

$$= 413.7 / 1.1 / (28)^{1/2} * 0.8 * 1.3 / 2.5 * 2.00 * 0.66 = 59.5 \text{ cm}$$

$$\text{Hooked } L_{dh} = 0.24 * f_y / (f_c)^{1/2} * db * 0.7 = 0.24 * 413.7 / (27.6)^{1/2} * 2.00 * 0.7 * 0.66 = 26.4 \text{ cm} \quad \text{ACI 12.5}$$

$$\text{Dev. length at toe side} = \text{Ftg} - \text{Heel} - \text{Cover} = (3.25 - 1.52) * 100 - 5.1 = 167.7 \text{ cm} > 59.5 \text{ cm} \quad \text{OK}$$

$$\text{Dev. length at heel side} = \text{Heel} - \text{Cover} = 1.52 * 100 - 5.1 = 146.9 \text{ cm} > 59.5 \text{ cm} \quad \text{OK}$$

$$A_s \text{ min} = \text{Min} (\text{Max} ((1.4 / f_y, 0.25 * \sqrt{f_c} / f_y) * b * d), 1.33 * A_s \text{ req})$$

ACI 10.5

$$= \text{Min} (\text{Max} ((1.4 / 414, 0.25 * (27.6)^{1/2} / 414) * 100 * 44.7, 1.33 * 6.6) = 13.8 \text{ cm}^2/\text{m}$$

$$\text{Min. steel area ratio} = A_s \text{ min} / A_s = 13.75 / 15.71 = 0.88 < 1.0 \quad \text{OK}$$

### TOE DESIGN (Comb. 1.2D+1.6(L+H))

$$\text{Bearing force} = (\text{Bearing1} + \text{Bearing2}) / 2 * \text{Toe} = (151.9 + 105.6) / 2 * 1.22 = 157.1 \text{ KN/m}$$

$$\text{Arm} = (\text{Bearing1} * \text{Toe}^2 / 2 + (\text{Bearing2} - \text{Bearing1}) * \text{Toe}^2 / 3) / \text{Force}$$

$$= (105.6 * 1.22^2 / 2 + (151.9 - 105.6) * 1.22^2 / 3) / 157.1 = 0.65 \text{ m}$$

$$\text{Moment} = 157.1 * 0.65 = 101.5 \text{ KN-m/m}$$

$$\text{Water Buoyancy} = \text{DL factor} * \gamma_w * \text{Water table} * \text{Toe} = 1.2 * 9.8 * 1.52 * 1.22 = 21.8 \text{ KN/m}$$

$$\text{Arm} = \text{Toe} / 2 = 1.22 / 2 = 0.61 \text{ m}$$

$$\text{Moment} = 21.8 * 0.61 = 13.3 \text{ KN-m/m}$$

$$\text{Concrete weight} = \text{DL factor} * \text{Thick} * \text{Toe} * \gamma_c = 1.2 * 50.8 / 100 * 1.22 * 24.00 = 17.8 \text{ KN/m}$$

$$\text{Arm} = \text{Toe} / 2 = 1.22 / 2 = 0.61 \text{ m}$$

$$\text{Moment} = 17.8 * 0.61 = 10.9 \text{ KN-m/m}$$

$$\text{Soil cover} = \text{DL factor} * \text{Toe} * \text{Height} * \gamma = 1.2 * 1.22 * 12.59 * 18.8 = 16.8 \text{ KN/m}$$

$$\text{Arm} = \text{Toe} / 2 = 1.22 / 2 = 0.61 \text{ m}$$

$$\text{Moment} = 16.8 * 0.61 = 10.2 \text{ KN-m/m}$$

$$\text{Max. Shear } V_u = 157.1 + 21.8 - 17.8 - 16.8 = 144.3 \text{ KN/m}$$

$$\text{Shear at crit. section } V_u = \text{Max shear} * (\text{Toe} - d) / \text{Toe} = 144.3 * (1.22 - 42.4 / 100) / 1.22 = 94.1 \text{ KN/m}$$

$$\text{Max. Moment } M_u = 101.5 + 13.3 - 10.9 - 10.2 = 93.7 \text{ KN/m}$$

$$\text{Shear strength } \phi V_n = \phi * 0.17 * (f_c)^{1/2} * 10 * d$$

ACI Eq. (11-3)

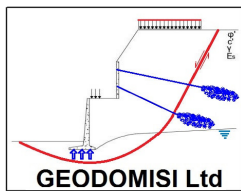
$$\phi V_n = 0.75 * 0.17 * (28)^{1/2} * 10 * 42.4 = 277.3 \text{ KN/m} > V_u = 94.1 \text{ KN/m} \quad \text{OK}$$

$$\text{Use D16 @ 20.0 cm} \quad A_s = 10.06 \text{ cm}^2/\text{m} \quad \rho = A_s / b d = 10.06 / (100 * 42.4) = 0.0024$$

$$\text{Bending strength } \phi M_n = \phi * d^2 * f_c * q * (1 - 0.59 * q)$$

ACI 10.2.7

$$\phi M_n = 0.90 * 42.4^2 * 27.6 * 0.036 * (1 - 0.59 * 0.036) = 155.6 \text{ KN-m/m} > M_u = 93.7 \text{ KN-m/m} \quad \text{OK}$$



## CANTILEVER RETAINING WALL DESIGN

Cover factor =  $Min(2.5, (Cover + db / 2, Spacing / 2) / db) = Min(2.5, (7.6 + 1.60 / 2, 20.0 / 2) / 1.60) = 2.5$

Straight  $Ld = fy / 1.1 / (fc)^{1/2} * Size * Location / Cover * db$  ACI Eq. (12-1)

=  $413.7 / 1.1 / (28)^{1/2} * 0.8 * 1.0 / 2.5 * 1.60 * 0.60 = 36.7 \text{ cm}$

Hooked  $Ldh = 0.24 * fy / (fc)^{1/2} * db * 0.7 = 0.24 * 413.7 / (27.6)^{1/2} * 1.60 * 0.7 * 0.60 = 21.2 \text{ cm}$  ACI 12.5

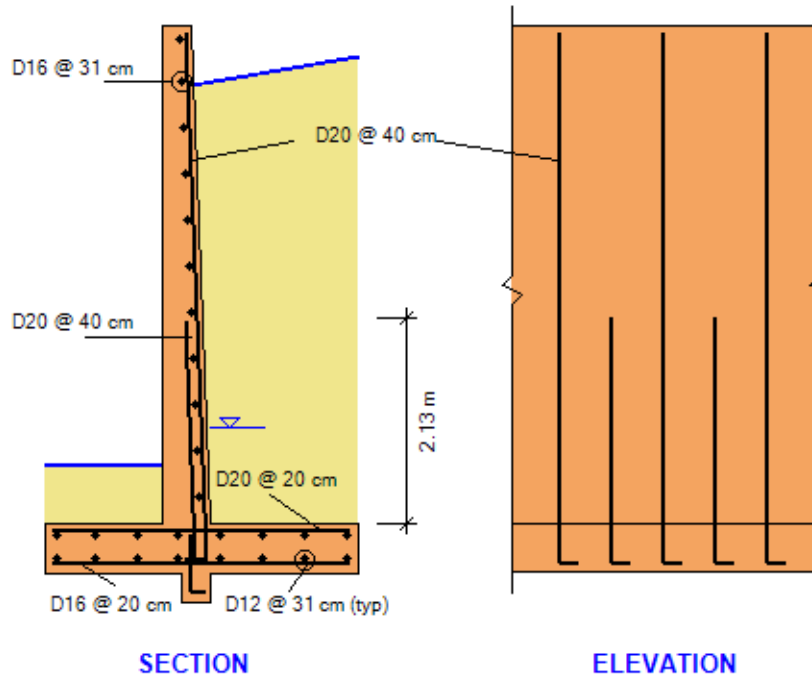
Dev. length at heel side =  $Ftg - Toe - Cover = (3.25 - 1.22) * 100 - 7.6 = 195.2 \text{ cm} > 36.7 \text{ cm}$  OK

Dev. length at toe side =  $Toe - Cover = 1.22 * 100 - 7.6 = 114.4 \text{ cm} > 36.7 \text{ cm}$  OK

$As_{min} = Min(Max((1.4 / fy, 0.25 * \sqrt{fc} / fy) * b * d), 1.33 * As_{req})$  ACI 10.5

=  $Min(Max(1.4 / 414, 0.25 * (27.6)^{1/2} / 414) * 100 * 42.4, 1.33 * 5.8) = 8.0 \text{ cm}^2/\text{m}$

Min. steel



### SHEAR KEY DESIGN (Comb. 0.9D+1.6H+E)

Shear key depth = 30.5 cm

Shear key thickness = 30.5 cm

Passive force =  $Lat \text{ factor} * (Passive1 + Passive2) / 2 * Key = 1.6 * (74.1 + 58.2) / 2 * 30.5 / 100 = 32.3 \text{ KN/m}$

Shear at crit. section  $Vu = Max \text{ shear} * (Key - d) / Key = 32.3 * (30.5 - 22.1) / 30.5 = 8.9 \text{ KN/m}$

$Arm = (Passive1 * Key^2 / 2 + (Passive2 - Passive1) * Key^2 / 3) / Force$

=  $(58.2 * 30.5^2 / 2 + (74.1 - 58.2) * 30.5^2 / 3) / 32.3 = 0.10 \text{ m}$

Max. moment  $Mu = 32.3 * 0.10 = 3.2 \text{ KN-m/m}$

Shear strength  $\phi Vn = \phi * 0.17 * (fc)^{1/2} * 10 * d$  ACI Eq. (11-3)

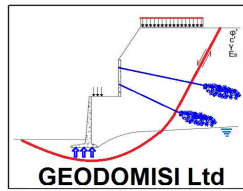
$\phi Vn = 0.75 * 0.17 * (28)^{1/2} * 10 * 22.1 = 144.4 \text{ KN/m} > Vu = 8.9 \text{ KN/m}$  OK

Use D16 @ 30.5 cm  $As = 6.60 \text{ cm}^2/\text{m}$   $\rho = As / b d = 6.60 / (100 * 22.1) = 0.0030$

Bending strength  $\phi Mn = \phi * d^2 * fc * q * (1 - 0.59 * q)$  ACI 10.2.7

$\phi Mn = 0.90 * 22.1^2 * 27.6 * 0.045 * (1 - 0.59 * 0.045) = 52.8 \text{ KN-m/m} > Mu = 3.2 \text{ KN-m/m}$  OK





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## CANTILEVER RETAINING WALL DESIGN

### DESIGN CODES

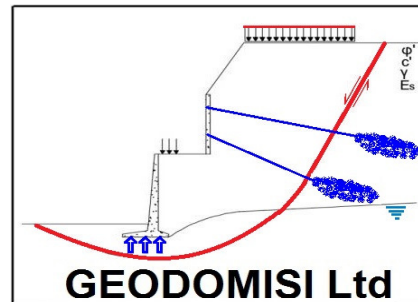
General Analysis .....	IBC-12
Concrete Design .....	ACI 318-11
Masonry Design .....	MSJC-11
Load Combinations .....	ASCE 7-05

### MATERIALS

	Stem	Footing	
Concrete $f_c$ ....	27.6	27.6	MPa
Rebars $f_y$ .....	413.7	413.7	MPa
Masonry $f_m$ ....	10.3		MPa

### LOAD COMBINATIONS (ASCE 7)

STABILITY	STRENGTH
① D+H+W	① 1.4D
② D+L+H+W	② 1.2D+1.6(L+H)
③ D+H+0.7E	③ 1.2D+0.8W
④ D+L+H+0.7E	④ 1.2D+L+1.6W
	⑤ 1.2D+L+E
	⑥ 0.9D+1.6H+1.6W
	⑦ 0.9D+1.6H+E



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